

Introduction to Controls Engineering  
Homework #5  
Assigned 3/6/13, Due: 3/13/13

Last PID problem

Design a PI controller for the first order system,  $G_p = \frac{1}{(.4 \text{ sec})s + 1}$  that gives a rise time of  $.5 \text{ sec}$  and a settling time of  $4 \text{ sec}$ .

Step One: cascade the PI controller,  $G_c = K_p + \frac{K_I}{s}$  with the plant and determine the closed loop transfer function,  $\frac{G_c G_p}{1 + G_c G_p}$ .

The denominator is second order, so equate coefficients between  $s^2 + 2\zeta\omega_n s + \omega_n^2$  (with  $\zeta$  and  $\omega_n$  determined from your performance specs) to calculate your  $K_p$  and  $K_I$ .

Using the matlab commands:

plant = tf(num,den)

and

step(plant)

plot the open loop response.

Using the matlab commands

control = tf(num,den)

and

step((control\*plant)/(1+control\*plant)))

plot the closed loop response.

NOTE: num and den are arrays of coefficients for the numerator and denominator of your transfer function. For instance num = [1 0], den = [2 1] translates into the transfer function  $\frac{s}{2s+1}$ . (Type "help tf" to get matlab's help on the function.)

How does your design compare against your performance specs?